

**MODELING THE EFFECT OF A NOVEL
AUTO-DISSEMINATION TRAP ON
THE SPREAD OF DENGUE IN HIGH-RISE
CONDOMINIA, MALAYSIA**

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In this paper, we use the classical Ross–Macdonald model to analyze the effect of the Mosquito Home System (MHS), which is an example of an auto-dissemination trap, in controlling the spread of dengue in Malaysia in a high-rise condominium environment. By using the national dengue data from Malaysia, we are able to estimate λ which represents the initial growth rate of the dengue epidemic and thus allows us to estimate the number of mosquitoes in Malaysia. The basic reproduction number R_0 is also obtained. We have constructed a mathematical expression which allows us to estimate the potential number of breeding sites for *Aedes* mosquitoes. Later on, by using the data available from the 11 months trials carried out in three blocks of flats in Selangor, we improved on our dengue

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model by including the effect of the MHS and thus modeling the impact it has on the spread of dengue within the flats. Numerical simulations and tables are also produced to illustrate our results.

Keywords: Dengue; Auto-Dissemination Trap; Mosquito Home System; Ordinary Differential Equations; Delayed Model; *Aedes Aegypti*; *Aedes Albopictus*; Numerical Simulations; Malaysia.

1. Introduction

Dengue is a vector-borne disease which is mainly transmitted by two types of *Aedes* mosquitoes, the main one for transmission is the *Aedes Aegypti* and the second one is *Aedes Albopictus*, where *Aedes Aegypti* mosquitoes are also responsible for the transmission of other diseases such as yellow fever and the zika virus.^{1–3} Dengue can be a life-threatening disease as infected individuals can develop severe dengue which includes dengue hemorrhagic fever. The World Health Organization has stated that every year there are around 50–100 million dengue infections where at least 100 countries have a dengue epidemic,² Malaysia being one of them.

Between 2014–2016, Malaysia had around 330,891 reported dengue cases with around 788 dengue-related deaths with a high incidence rate of 396.4 per 100,000 population in 2015 causing Malaysia to suffer from serious economic and health burdens. In the study carried out by Packierisamy *et al.*,⁴ it is estimated that in 2010, it had cost Malaysia around USD \$73.45 million in dengue-related vector control which was around USD \$2.63 per capita population. As a result, it is crucial that we find a way to control the spread of dengue in Malaysia. One of the main ways which Malaysia has used to battle against dengue is to use outdoor space spraying commonly known as chemical fogging. However, space spraying is most effective one month after the spraying has taken place and the effect will reduce over time.⁵ In addition, space spraying is a passive approach as spraying will take place only in areas where dengue cases have been reported. One of the main challenges in controlling the spread of dengue is that it is often difficult to find all breeding sites of *Aedes* mosquitoes. As a result, there is a new method by which we could overcome the problem, namely the Mosquito Home System (MHS) which is an auto-dissemination trap. The mosquito trap is called an auto-dissemination trap because it contains a solution which the mosquitoes disseminate to other breeding sites. The MHS is a container which contains a special solution that will attract the female *Aedes* mosquitoes to lay their eggs within the container. Furthermore, any eggs that are laid inside the MHS will get killed off by the solution inside thus preventing those eggs from hatching into adult *Aedes* mosquitoes. In other words, the MHS will be able to reduce the *Aedes* mosquito population available to transmit the dengue virus. Before we can conclude on the effectiveness of the MHSs in reducing the number of dengue cases, it is crucial for us to analyze in detail the effect of using the MHS. As a result, in this paper, we will use the well-known classical Ross–Macdonald model⁶ to describe the spread of dengue between humans and

Aedes mosquitoes in Malaysia. Most importantly, we will also perform mathematical modeling to investigate the impact of the MHSs on reducing the *Aedes* population and thus reduce the number of dengue cases. In order to improve on the accuracy and the reliability of our analysis, it is important to point out that we will be using the actual experimental field data obtained from deploying the MHSs in three highly urbanized residential condominiums known as Ridzuan Court Sunway in Selangor of Malaysia,⁷ where the area is responsible for about 60% of the total dengue cases in Malaysia.

This paper is arranged as follows: In Sec. 2, we will introduce the classical Ross–Macdonald model as well as the basic reproduction number. In Sec. 3, we will mathematically estimate the number of potential breeding sites of *Aedes* mosquitoes and perform some basic analysis on the effect of using the MHSs in reducing the number of dengue cases in the trial site. In Sec. 4, we constructed a list of different biting probabilities corresponding to different amounts of time spent outdoors. In Sec. 5, we will perform thorough analysis on the effect of having different levels of MHSs on the number of dengue cases in those three high-rise condominiums. Lastly in Sec. 6, we will summarize all our results. Numerical simulations and tables are produced throughout the paper to illustrate our findings.

2. The Dengue Model and the Basic Reproduction Number

Let us consider the following delayed SIR model for dengue mentioned in Ref. 8:

$$\begin{aligned}
 \frac{dS_H(t)}{dt} &= -abI_v(t)\frac{S_H(t)}{N_H} - \mu_H S_H(t) + \mu_H N_H, \\
 \frac{dI_H(t)}{dt} &= abI_v(t)\frac{S_H(t)}{N_H} - (\mu_H + \gamma)I_H(t), \\
 \frac{dR_H(t)}{dt} &= \gamma I_H(t) - \mu_H R_H(t), \\
 \frac{dS_v(t)}{dt} &= -acS_v(t)\frac{I_H(t)}{N_H} - \mu_v S_v(t) + \mu_v N_v, \\
 \frac{dL_v(t)}{dt} &= acS_v(t)\frac{I_H(t)}{N_H} - \mu_v L_v(t) - acS_v(t - \tau)\frac{I_H(t - \tau)}{N_H}e^{-\mu_v \tau}, \\
 \frac{dI_v(t)}{dt} &= acS_v(t - \tau)\frac{I_H(t - \tau)}{N_H}e^{-\mu_v \tau} - \mu_v I_v(t),
 \end{aligned}
 \tag{2.1}$$

with initial conditions $S_H(0), I_H(0)$ and $R_H(0)$, where $S_H(t), I_H(t)$ and $R_H(t)$ represent, respectively the susceptible, infected and recovered humans, while $S_v(0), L_v(0)$ and $I_v(0)$ denote the initial conditions for $S_v(t), L_v(t)$ and $I_v(t)$ which represent, respectively the susceptible, latent and infected mosquitoes. Note that $N_H = S_H + I_H + R_H$ denotes the total population size for humans and $N_v = S_v + L_v + I_v$ represents the total population for *Aedes* mosquitoes where

they are both constant. a represents the biting rate for *Aedes* mosquitoes, b is the dengue transmission probability when an infectious mosquito bites a susceptible human and c is the dengue transmission probability when a susceptible mosquito bites an infected human. μ_H and μ_v are the per capita mortality rates for humans and *Aedes* mosquitoes, respectively. γ is the per capita human recovery rate and τ is the dengue extrinsic incubation period.

In Eq. (2.1), some of the parameters are easy to estimate. For example μ_H is the reciprocal of the average human lifetime. Similarly μ_v is the reciprocal of the average mosquito lifetime and γ is the reciprocal of the infectious period. Other parameters such as N_v , the total number of mosquitoes, are more difficult to estimate. However, we also have data on the initial phase of the epidemic and can use this to estimate λ , the initial exponential growth rate of the number of dengue cases, by fitting a function $Ae^{\lambda t}$, where A is a constant, to the initial stage of an epidemic. From this λ estimate, we can find the basic reproduction number R_0 , and from R_0 , we can estimate N_v . (Recall that R_0 represents the expected number of secondary cases that will arise from a single infected person entering a disease-free population at equilibrium. Alternatively, R_0 can be thought of as the expected number of secondary cases that will arise from a single infected mosquito entering a disease-free population at equilibrium.)

The Appendix of Ref. 9 gives a method to estimate R_0 for a very similar model from the easily estimated parameters λ , μ_H , μ_v , τ and γ , by looking at the initial exponential phase of the number of dengue cases. We shall use this method to estimate R_0 for our model (see Eq. (2.4)). Then we shall give an alternative expression for R_0 , Eq. (2.5), derived from the differential equation model, Eqs. (2.1), and use it to estimate m , the number of *Aedes* mosquitoes per human, and hence to estimate N_v , the total number of mosquitoes.

We apply the estimation method in the Appendix of Ref. 9 to our model. Our model is similar to the model discussed in Ref. 9 but additionally includes both the per capita human death rate, μ_H , and the transmission probability per bite from an infected human to a susceptible mosquito, c . Moreover there is a mistake in the R_0 calculation in Ref. 9. In the second equation of each of Eqs. (9) and (10) in Ref. 9, the argument of i_H , which is not explicitly stated, should be $t - \tau$ (not t). Following the method outlined in Ref. 9 gives

$$R_0 = \left(1 + \frac{\lambda^2 + \lambda(\mu + \gamma)}{\mu\gamma}\right) e^{\lambda\tau}, \quad (2.2)$$

$$\text{not } R_0 = \left(1 + \frac{\lambda^2 + \lambda(\mu + \gamma)}{\mu\gamma}\right). \quad (2.3)$$

So the R_0 value stated in Ref. 9 is (2.3) but it should be (2.2). Note that μ in Ref. 9 corresponds to μ_v in our model.

Applying the same method to our model, it is straightforward to obtain

$$R_0 = \frac{(\lambda + \mu_v)(\lambda + \mu_H + \gamma)e^{\lambda\tau}}{(\mu_H + \gamma)\mu_v}. \tag{2.4}$$

In order to calculate the basic reproduction number, we need to know the parameter values. According to the World Bank data,¹⁰ the life expectancy in Malaysia in 2015 was 75 years and thus $\mu_H = 1/(75 \times 365)$ per day. The average lifespan for an *Aedes* mosquito is around 2 weeks according to the Singapore National Environment Agency¹¹ and thus $\mu_v = 1/14$ per day. The human recovery rate is $\gamma = 1/7$ per day and the extrinsic incubation period is around 8 days.¹²

By using the dengue data available in Ref. 13 which contains the number of dengue cases in Malaysia in 2013, and by using numerical simulation in R, we have plotted an exponential curve fitted against the real data to estimate λ , which recall represents the initial growth rate of the dengue epidemic. In this case, we have that $\lambda = 0.0053/\text{day}$. By substituting all the required parameter values into Eq. (2.4), we have that $R_0 = 1.162$.

One of the main difficulties when modeling the spread of dengue is that it is extremely difficult to know the number of *Aedes* mosquitoes that are in the country. However, we can estimate this using an alternative definition of the basic reproduction number which is expressed in terms of m , where $m = N_v/N_H$ is the number of *Aedes* mosquitoes per one human. The basic reproduction number derived from the differential equation model (2.1) is given as follows:

$$R_0 = \frac{ma^2bce^{-\mu_v\tau}}{\mu_v(\mu_H + \gamma)}, \tag{2.5}$$

where $a = 0.25$ is the *Aedes* mosquitoes daily biting rate, $b = 0.75$ and $c = 0.375$.¹⁴ Similarly by substituting the parameter values and setting $R_0 = 1.162$, it is clear that $m = 1.195$. As a result, the number of *Aedes* mosquitoes can be estimated using $N_v = mN_H$. Note that both Eqs. (2.4) and (2.5) represent the basic reproduction number, but they are derived in different ways.

In the next section, we will focus on analyzing the effect of the MHS on the spread of dengue within the three blocks of flats in Selangor where an 11 months MHS trial has been carried out.

3. The Effect of the MHS on the Flats

Throughout this paper, unless stated otherwise, all figures will be rounded to three decimal places with the unit of time in weeks.

In order to analyze the effect of the MHS on the spread of dengue within the flats, we will modify the delayed dengue model (2.1) into a more complicated one where we are now working with 12 differential equations, where six of them describe the disease dynamics in Kuala Lumpur (KL) while the other six represent the dynamics

of the disease within the flats with the effect of the MHS. Let us define the new model as follows:

$$\begin{aligned} \frac{dS_{H_1}(t)}{dt} &= -abI_{v_1}(t)\frac{S_{H_1}(t)}{N_{H_1}} - \mu_H S_{H_1}(t) + \mu_H N_{H_1}, \\ \frac{dI_{H_1}(t)}{dt} &= abI_{v_1}(t)\frac{S_{H_1}(t)}{N_{H_1}} - (\mu_H + \gamma)I_{H_1}(t), \\ \frac{dR_{H_1}(t)}{dt} &= \gamma I_{H_1}(t) - \mu_H R_{H_1}(t), \end{aligned} \tag{3.1}$$

$$\begin{aligned} \frac{dS_{v_1}(t)}{dt} &= -acS_{v_1}(t)\frac{I_{H_1}(t)}{N_{H_1}} - \mu_v S_{v_1}(t) + \mu_v N_{v_1}, \\ \frac{dL_{v_1}(t)}{dt} &= acS_{v_1}(t)\frac{I_{H_1}(t)}{N_{H_1}} - \mu_v L_{v_1}(t) - acS_{v_1}(t - \tau)\frac{I_{H_1}(t - \tau)}{N_{H_1}}e^{-\mu_v \tau}, \\ \frac{dI_{v_1}(t)}{dt} &= acS_{v_1}(t - \tau)\frac{I_{H_1}(t - \tau)}{N_{H_1}}e^{-\mu_v \tau} - \mu_v I_{v_1}(t), \\ \frac{dS_{H_2}(t)}{dt} &= -ab\left(P\frac{I_{v_1}(t)}{N_{H_1}} + (1 - P)\frac{I_{v_2}(t)}{N_{H_2}}\right)S_{H_2}(t) - \mu_H S_{H_2}(t) + \mu_H N_{H_2}, \\ \frac{dI_{H_2}(t)}{dt} &= ab\left(P\frac{I_{v_1}(t)}{N_{H_1}} + (1 - P)\frac{I_{v_2}(t)}{N_{H_2}}\right)S_{H_2}(t) - (\mu_H + \gamma)I_{H_2}(t), \\ \frac{dR_{H_2}(t)}{dt} &= \gamma I_{H_2}(t) - \mu_H R_{H_2}(t), \end{aligned} \tag{3.2}$$

$$\begin{aligned} \frac{dS_{v_2}(t)}{dt} &= -acS_{v_2}(t)\frac{I_{H_2}(t)}{N_{H_2}} - \mu_v S_{v_2}(t) + \mu_v N_{v_2}(1 - P^*), \\ \frac{dL_{v_2}(t)}{dt} &= acS_{v_2}(t)\frac{I_{H_2}(t)}{N_{H_2}} - \mu_v L_{v_2}(t) - acS_{v_2}(t - \tau)\frac{I_{H_2}(t - \tau)}{N_{H_2}}e^{-\mu_v \tau}, \\ \frac{dI_{v_2}(t)}{dt} &= acS_{v_2}(t - \tau)\frac{I_{H_2}(t - \tau)}{N_{H_2}}e^{-\mu_v \tau} - \mu_v I_{v_2}(t), \end{aligned}$$

where all the parameters are defined as before and Eq. (3.1) represent the transmission of dengue between humans and *Aedes* mosquitoes in KL, while Eq. (3.2) represent the transmission of dengue within the three blocks of flats. The parameter P denotes the fraction of time in which an average person resident in the flats stays in KL, while $1 - P$ represents the fraction of time an average person stays inside the flats. P^* represents the total reduction in the proportion of *Aedes* mosquitoes population as a result of using the MHS inside the three blocks of flats.

Before we solve the 12 differential equations using R, it is useful to estimate the potential number of mosquito sites that are in the vicinity of the flats, in order to determine the appropriate number of MHSs that would be needed to achieve a substantial effect in reducing the number of dengue cases.

From a previous trial carried out in the Jacob-Ballas Childrens' Park at Singapore Botanic Gardens,¹⁵ we know that there were 46 MHSs and 46 Gravitrap traps used to collect *Aedes* eggs. A Gravitrap is a simple cylindrical black container with sticky surface which allows the female *Aedes* mosquitoes to lay their eggs.¹⁶ Note that the Gravitrap traps used do not contain the special solution which lures the female *Aedes*. The total number of eggs collected by the MHSs were approximately 12 times more than the ones collected by the Gravitrap traps. An increase is to be expected as the MHS has a special chemical within the trap that naturally attracts *Aedes* mosquitoes to lay eggs within it.

In the absence of any information to the contrary, we assume that without the MHSs the mosquitoes choose one of the available breeding sites at random to lay their eggs. However, we know that at the Jacob-Ballas Childrens' Park in the Singapore Botanic Gardens trial, the MHSs were approximately 12 times as attractive to mosquitoes as the Gravitrap traps, which are the only other available breeding sites on which we have information. Hence we assume that the MHSs are 12 times more attractive than other potential breeding sites. Let us assume that there are x MHSs being deployed, o ovitraps and y hidden breeding sites. Then the probability that an egg is laid in one of the x MHSs is

$$\frac{12x}{12x + o + y} \tag{3.3}$$

As there are k eggs altogether, then the total expected number of eggs laid in the MHSs is

$$k \times \frac{12x}{12x + o + y} = \frac{12kx}{12x + o + y} \tag{3.4}$$

So this is the expected number of eggs collected by the MHSs within the three blocks of flats. This will be used later on in Eq. (3.6) to estimate the number of breeding sites.

From Fig. 6 in Ref. 7, we have that the mean number of eggs per paper collected in all three blocks of flats using the MHS has decreased to around 70.65% of its value before introduction after extra MHSs were introduced into block B thus increasing the total number of MHSs deployed in the flats from 344 to 552. Each of the MHSs contains a piece of tissue paper which dips into the solution and the mosquitoes lay their eggs on it. Therefore the mean number of hidden breeding sites can be estimated, as the mean number of eggs per paper can be expressed as follows:

$$\frac{1}{x} \times \frac{12kx}{12x + o + y} = \frac{12k}{12x + o + y} \tag{3.5}$$

As a result,

$$\frac{0.7065 \times 12k}{12 \times 344 + 356 + y} = \frac{12k}{12 \times 552 + 356 + y}, \tag{3.6}$$

as $o = 356$. By re-arranging Eq. (3.6) and solving for y , which represents the number of hidden sites, we have that $y = 1524$. This means that on average each block of

flats has around 505 breeding sites of *Aedes* mosquitoes. This possibly explains why initially having 344 MHSs in all blocks of flats, in other words around 114 MHSs in each block has very little effect on reducing the Ovitrap Index as it is relatively low compared to our estimated number of *Aedes* sites. However as soon as the number of MHSs in block B was increased from the initial 116 to 324, we see a drastic decrease in Ovitrap Index as obviously the number of MHSs used in block B is more than half of the potential breeding sites associated with that block, assuming that the breeding sites are equally distributed among the blocks.

We will now solve the differential equations given by Eqs. (3.1) and (3.2) and produce some numerical simulations to demonstrate graphically what happened to the dynamics of dengue.

Example 3.1. Let us define all the parameter values the same as before but changing the *Aedes* mosquitoes' daily biting rate to 0.20 and thus m would become 1.867. According to the data given in Ref. 17, the total population in KL in 2013 is around 1,720,000 and thus the estimated number of *Aedes* mosquitoes using the relation that $N_v = mN_H$ is around 2,055,632. Each block of flats has 10 units of houses per floor and thus in total there will be 800 units of houses in all three blocks of flats. By assuming that each house has an average of four residents, then $N_{H_2} = 3,200$ and $N_{v_2} = 3,824.432$.

The incidence rate in KL in 2013 was 146.7 per year per 100,000 population.¹⁸ Typically, dengue cases have a low ratio of symptomatic to asymptomatic cases of 1 to 4, respectively and thus we will increase the incidence rate by 5 times to reflect this situation. In addition, from 1995 to 2012, the number of dengue cases in Malaysia was around 505,264 (without taking into consideration the asymptomatic cases). From previous data on the number of reported dengue cases in different states in Malaysia, KL is responsible for around 3–10% of those cases. Therefore, by assuming that KL is responsible for around 5% of those dengue cases and assuming that everyone was infected by the same serotype, we can estimate the number of recovered individuals in 2013. The unit of time, unless stated otherwise, is in weeks.

Let us define the initial values of Eqs. (3.1) and (3.2) to be

$$\begin{aligned}
 S_{H_1}(0) &= 1,593,441, & I_{H_1}(0) &= 242.619, & R_{H_1}(0) &= 126,316, \\
 S_{v_1}(0) &= 3,211,447, & L_{v_1}(0) &= 207.042, & I_{v_1}(0) &= 268.608, \\
 S_{H_2}(0) &= 2,964.542, & I_{H_2}(0) &= 0.451, & R_{H_2}(0) &= 235.007, \\
 S_{v_2}(0) &= 5,974.785, & L_{v_2}(0) &= 0.385, & I_{v_2}(0) &= 0.4997,
 \end{aligned}$$

where we have set the initial values within the flats to reflect the distribution of the initial values in KL. Note that the initial conditions for the number of susceptible, latent and infected mosquitoes in KL are obtained using the initial values of $I_{H_1}(0)$ and N_{H_1} and substituting them into the differential equations for $\frac{dS_{v_1}(t)}{dt}$, $\frac{dL_{v_1}(t)}{dt}$ and $\frac{dI_{v_1}(t)}{dt}$.

It is known that the *Aedes* mosquito bites more often at dawn and dusk,¹⁹ therefore people are most likely to stay indoors during those periods, and thus it is reasonable to assume that P is relatively small, say $P = 0.10$, where recall that P is the proportion of time that an average person resident in the flats is in KL.

From the Singapore Park data,¹⁵ we know that during the two months trial, the total reduction in the *Aedes* population was around 0.5889, and thus by using this as a rough guide, we will set $P^* = 0.5889$.

The numerical simulations for the spread of dengue in KL are shown in Fig. 1 including the incidence cases and the total number of cases over a period of three years.

The numerical simulation for the number of incidence cases in weeks and the total number of dengue cases within the blocks of flats is given in Fig. 2. The red lines shown in both figures represent the effect of using the MHSs in the flats and thus reducing the *Aedes* mosquitoes population by a factor of 0.5889. The black line represents the effect of having no MHSs present within the blocks of flats. From Fig. 2, it is clear that the MHSs have effectively reduced the number of dengue incidences. This is also confirmed in simulation (b) of Fig. 2 where we have seen

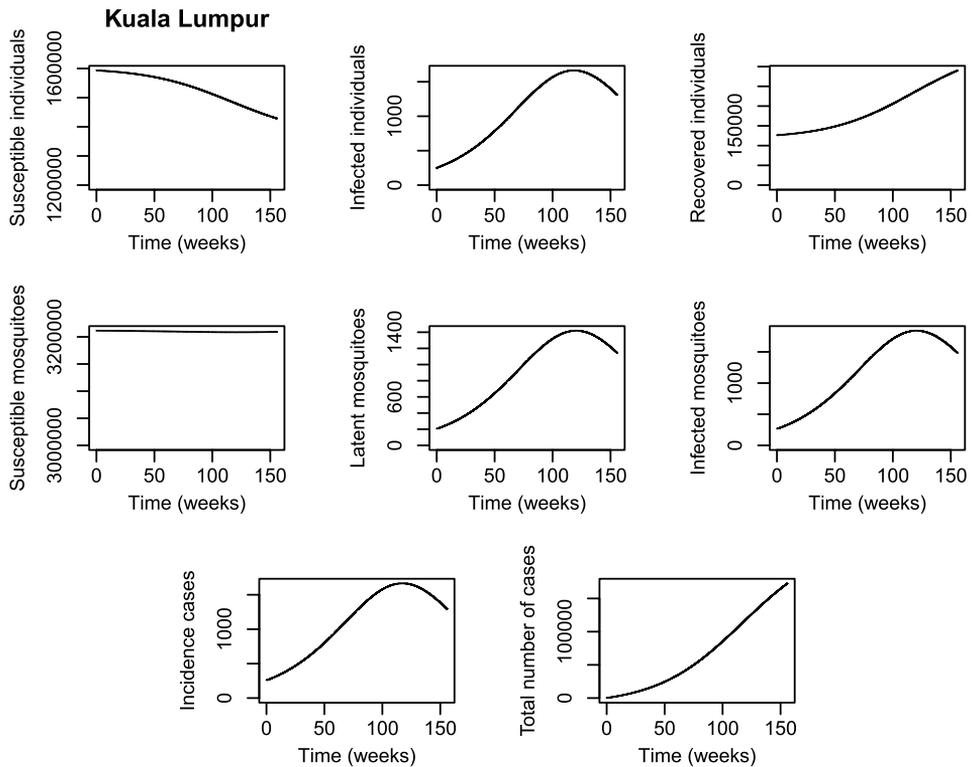


Fig. 1. Numerical simulation for our solution to Eq. (3.1) over a period of three years.

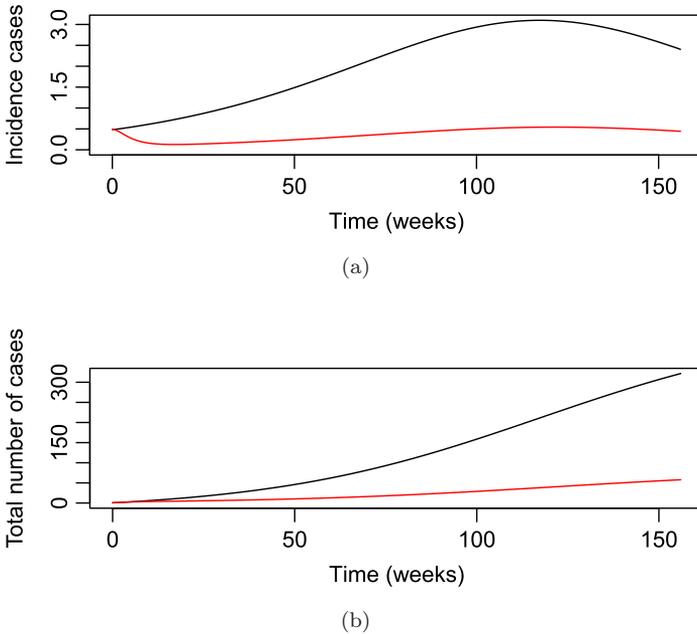


Fig. 2. Numerical simulation for (a) number of incidence cases per week and (b) total number of cases within the blocks of flats with $P = 0.10$ where the black line and red line represent $P^* = 0$ and $P^* = 0.5889$ respectively over a period of three years.

the total number of cases over a period of three years have reduced drastically as a result of using the MHSs within the blocks of flats. Note that we have also produced the numerical simulation for the number of infected individuals within the blocks of flats, however the simulation has the same qualitative behavior as the number of dengue incidence cases per week shown. Therefore we have decided to omit the simulation in Fig. 2. This is the case throughout the paper for other similar simulations.

The dynamical behavior for the *Aedes* mosquitoes within the flats is illustrated in Fig. 3, where the red line represents the effect from the MHSs and the black line represents the effect when we have no MHSs. Again the effect is clear as shown in the simulations. Note also that the numerical simulation for the number of latent *Aedes* mosquitoes was also produced, however the simulation has the same qualitative behavior as the number of infected *Aedes* mosquitoes shown. Therefore we have omitted the latent mosquitoes figure in Fig. 3. This is the case throughout the paper for other similar simulations.

From Table 1, we can see clearly that by introducing the MHSs in the three blocks of flats, not only did the mean number of infected *Aedes* mosquitoes reduce by a high proportion of 87.87%, the mean number of infected individuals has also decreased dramatically by about 78.04%. In addition, the mean number of dengue incidence cases has reduced by 78.94%. These results are very promising, as they

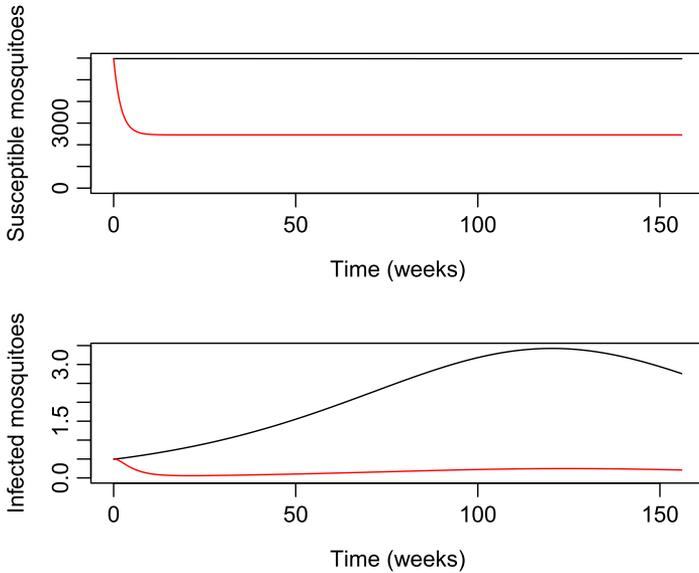


Fig. 3. Dynamical behavior of *Aedes* mosquitoes within the blocks of flats with $P = 0.10$ and the black line and red line represent $P^* = 0$ and $P^* = 0.5889$ respectively over a period of three years.

Table 1. Mean values for variables in flats with and without the MHSs to 3 d.p after one year where $P = 0.10$.

Variable values	$P^* = 0$	$P^* = 0.5889$	Percentage change
Susceptible individuals $S_{H_2}(t)$ in flats	2,946.55	2,960.778	Increased by 0.48%
Infected individuals $I_{H_2}(t)$ in flats	0.912	0.200	Decreased by 78.04%
Recovered individuals $R_{H_2}(t)$ in flats	252.538	239.022	Decreased by 5.35%
Susceptible <i>Aedes</i> mosquitoes $S_{v_2}(t)$ in flats	5,973.959	2,591.714	Decreased by 56.62%
Infected <i>Aedes</i> mosquitoes $I_{v_2}(t)$ in flats	0.966	0.117	Decreased by 87.87%
Latent <i>Aedes</i> mosquitoes $L_{v_2}(t)$ in flats	0.745	0.09	Decreased by 87.92%
Incidence cases	0.933	0.196	Decreased by 78.94%
Total cases	48.984	10.696	Decreased by 78.16%

highlight the fact that the MHSs have effectively reduced the number of dengue cases within the flats by reducing the number of *Aedes* mosquitoes. Furthermore, the impact ratio which can be calculated using

$$1 - \frac{\text{cases after}}{\text{cases before}},$$

Table 2. Endemic equilibrium values for variables in flats with and without the MHSs to 3 d.p where $P = 0.10$.

Variable values	$P^* = 0$	$P^* = 0.5889$	Percentage change
Susceptible individuals in flats $S_{H_2}(t)$	2,753.155	3,113.127	Increased by 13.07%
Infected individuals in flats $I_{H_2}(t)$	0.115	0.022	Decreased by 80.87%
Recovered individuals in flats $R_{H_2}(t)$	446.730	86.850	Decreased by 80.56%
Susceptible <i>Aedes</i> mosquitoes in flats $S_{v_2}(t)$	5,975.446	2,456.580	Decreased by 58.89%
Infected <i>Aedes</i> mosquitoes in flats $I_{v_2}(t)$	0.127	0.010	Decreased by 92.13%
Latent <i>Aedes</i> mosquitoes in flats $L_{v_2}(t)$	0.098	0.008	Decreased by 92.84%
Incidence cases	0.115	0.022	Decreased by 80.87%
Total cases (per year)	5.958	1.158	Decreased by 80.56%

shows that the impact of introducing the MHSs in the three blocks of flats has a value of 0.7816.

Note that the mean number of susceptible individuals within the flats have increased when we have the MHSs, this is possibly due to the fact that the rate of infection is slowing down as there are now less *Aedes* mosquitoes to spread the dengue virus.

The corresponding endemic equilibrium values for the number of infected individuals, incidence cases and total dengue cases within the blocks of flats with and without using the MHSs are shown in Table 2. The results shown in Table 2 further highlight the impact of using the MHSs.

Note that the cumulative number of dengue cases in KL in 2013 over a period of 40 weeks was 8420 (after multiplying 1684^{20} by 5 to take into consideration asymptomatic cases). From our numerical simulations given in Example 3.1, we have that the total number of cases after 40 weeks is around 17,323.918. To further investigate this scenario, we run the simulations for a longer period of time until the end of 2015. The cumulative number of dengue cases in Malaysia from 2013 to 2015 was 272,880. By making the same assumption that KL was responsible for 5% of the overall dengue cases in Malaysia in 2015, then from 2013 to 2015, KL had around 68,220 dengue cases (after multiplying 13,644 by 5 to take into consideration asymptomatic cases). From our numerical simulation, at the end of 2015, we expect to have 91,548.72 which is around 1.34 times more than the actual number of cases.

Although it seems that our numerical simulation has over-predicted the actual dengue data by around 1.34 times, it is important to note that this could be due to the symptomatic to asymptomatic cases ratio that we chose in Example 3.1. Note

that the estimation of this ratio varies greatly. For example, Ref. 21 used the ratio of 1:3.9 for the symptomatic to asymptomatic cases ratio which is very close to the 1:4 ratio that we used in the previous example, while in Ref. 22, Wilder-Smith *et al.* have chosen the symptomatic to asymptomatic cases ratio for the dengue cases in Singapore to range from 1:2.1 to 1:10. As a result, it would be interesting to know what would happen if we choose a different symptomatic to asymptomatic cases ratio than the one in Example 3.1. The results are shown in the following example.

Note that from the official report from the Ministry of Health in Malaysia, Ref. 20, the cumulative dengue cases in KL in 2013 over a period of 40 weeks was 1684, but by using the incidence rate in KL in 2013, namely 146.7 per 100,000,¹⁸ the number of reported cases should be around 1940.90. The difference could be due to not having the exact number of population of KL.

Example 3.2 (1:9 ratio). By choosing the symptomatic to asymptomatic cases ratio for dengue to be 1:9, the new initial values of Eqs. (3.1) and (3.2) are

$$\begin{aligned}
 S_{H_1}(0) &= 1,466,883, & I_{H_1}(0) &= 485.239, & R_{H_1}(0) &= 252,632, \\
 S_{v_1}(0) &= 3,210,972, & L_{v_1}(0) &= 414.022, & I_{v_1}(0) &= 537.136, \\
 S_{H_2}(0) &= 2,729.084, & I_{H_2}(0) &= 0.903, & R_{H_2}(0) &= 470.013, \\
 S_{v_2}(0) &= 5,973.901, & L_{v_2}(0) &= 0.770, & I_{v_2}(0) &= 0.999,
 \end{aligned}$$

where all the parameter values are defined as before.

By carrying out the same numerical simulations as in Example 3.1, we have that the cumulative number of cases in KL over the first 40 weeks in 2013 was 17,959.94. The actual cumulative number of dengue cases in KL over the same period was 16,840 (after multiplying 1,684²⁰ by 10 to take asymptomatic cases into consideration). Similarly to before, we continue the simulation for a longer period of time until the end of 2015 to get the total number of cases in KL to be 37,897. The actual dengue cases data at the end of 2015 was 136,440 (after multiplying 13,644 by 10 to take into consideration asymptomatic cases). As a result, for this ratio, our estimated total number of dengue cases is around 3.6 times less than the actual dengue cases. This could be due to the fact that the dengue incidence rate in 2015 was about 2.72 times more than the one in 2013.

By comparing the results from two different symptomatic to asymptomatic ratios, it seems that a 1:4 ratio gives a more accurate result when comparing the estimated data with the actual dengue data given in Ref. 20. Therefore, for the rest of the paper, we will continue the analysis by assuming that the symptomatic to asymptomatic ratio is 1:4.

Note that the absolute numbers of infected individuals and infected and latent mosquitoes in the flats are very small (less than one) as shown in Tables 1 and 2. Hence at these levels of small numbers of infected individuals and mosquitoes, a

deterministic model strictly speaking should not be used and a stochastic model would be preferable. Nonetheless, the deterministic model can still give insight into the behavior of the system, particularly when comparing the number of cases in the flats with and without the MHSs or later (in Sec. 4) when comparing the equilibrium values with different values of P .

Note also that the number of dengue cases in KL will be large so for that part of the model a deterministic model is appropriate. As the disease is endemic in KL, there is a constant source of infection from outside the flats. So the disease will not die out in the flats.

4. Proportion of Time Outdoors

Recall from Sec. 3 that P denotes the fraction of time in which an average person resident in the flats stays in KL and P^* represents the total reduction in the proportion of *Aedes* mosquitoes as a result of the MHSs. From the simulations carried out, it is clear that the two parameter values P and P^* play an important role in controlling the spread of dengue within the flats. Therefore in the next two sections, we will focus on these two parameter values.

First of all, we will look at the effect of having different P values. In this section, we will use the biting facts on *Aedes* mosquitoes and interpret P in a slightly different way where P represents the proportion of bites a person will get if going outdoors in a given time interval and thus $1 - P$ represents the proportion of bites if a person remains inside. The values of P will thus vary depending on the time the person decides to go out. From the biting facts data available collected in April 2007, the three time slots which have the highest *Aedes*' biting activity are between 6–6.45 am, 5–5.45 pm and 6–6.45 pm as mosquitoes are more likely to bite at dusk and dawn.

From Table 3, we have five different time slots in which a person decides to leave the house and be in KL and remain indoors with their corresponding P and $1 - P$ values, respectively.

By keeping the parameter values the same as in Example 3.1 where $P^* = 0.5889$ and solving the differential equations for different P values, we have the results shown in Table 4 at the end of one year. From Table 4, it is clear that as P decreases, the number of incidence cases, the total number of dengue cases, infected individuals

Table 3. Proportions of *Aedes* bites according to biting activities at different time intervals.

Outdoor Time	P (outdoor)	$1 - P$ (indoor)
6 am–7.45 pm	0.6610	0.3390
6 am–6.45 pm	0.6210	0.3790
9 am–7.45 pm	0.4770	0.5230
8 am–5.45 pm	0.3190	0.6810
9 am–4.45 pm	0.1280	0.8720

Table 4. Mean values for variables in flats for various values for P with $P^* = 0.5889$ to 3 d.p after one year.

Variable values	$P = 0.6610$	$P = 0.6210$	$P = 0.4770$	$P = 0.3190$	$P = 0.1280$
Susceptible individuals in flats	2,950.584	2,951.141	2,953.324	2,956.094	2,960.113
Infected individuals in flats	0.714	0.686	0.578	0.439	0.234
Recovered individuals in flats	248.702	248.173	246.098	243.467	239.652
Susceptible <i>Aedes</i> mosquitoes in flats	2,591.326	2,591.347	2,591.429	2,591.534	2,591.688
Infected <i>Aedes</i> mosquitoes in flats	0.336	0.324	0.278	0.219	0.132
Latent <i>Aedes</i> mosquitoes in flats	0.259	0.250	0.214	0.168	0.101
Incidence cases	0.728	0.699	0.587	0.439	0.232
Total cases in flats	38.331	36.848	31.010	23.533	12.532

and infected *Aedes* mosquitoes in flats also decrease accordingly. A smaller P value means that an individual is outside in KL at a time when *Aedes* mosquitoes are not as active. As a result, it is reasonable to notice a decrease in incidence rate and infected cases as the chance of a susceptible individual bringing in new infection into the flat will be relatively lower compared to a higher P value.

The corresponding endemic equilibrium values for when $P^* = 0.5889$ for different values of P are shown in Table 5. We can see that as P decreases, the endemic equilibrium values for the total number of dengue cases within the flats also decrease.

Table 5. Endemic equilibrium values for variables in flats with different P values where $P^* = 0.5889$ to 3 d.p.

Variable values	$P = 0.6610$	$P = 0.6210$	$P = 0.4770$	$P = 0.3190$	$P = 0.1280$
Susceptible individuals in flats	2,843.632	2,856.567	2,908.634	2,978.761	3,092.447
Infected individuals in flats	0.091	0.088	0.074	0.057	0.028
Recovered individuals in flats	356.277	343.345	291.291	221.182	107.526
Susceptible <i>Aedes</i> mosquitoes in flats	2,456.524	2,456.527	2,456.538	2,456.552	2,456.576
Infected <i>Aedes</i> mosquitoes in flats	0.042	0.040	0.034	0.026	0.013
Latent <i>Aedes</i> mosquitoes in flats	0.032	0.031	0.026	0.020	0.010
Incidence cases	0.091	0.088	0.075	0.057	0.028
Total cases (per year)	4.752	4.579	3.885	2.950	1.434

5. Different Numbers of MHSs Within the Flats

In this section, we will focus on analyzing the effect of having different number of MHSs on the spread of dengue, in particular we will look at three different cases, namely

- (1) No MHSs within the flats,
- (2) 344 MHSs and 356 ovitraps within the flats,
- (3) 552 MHSs and 356 ovitraps within the flats.

Recall that P^* represents the total reduction in the proportion of *Aedes* mosquitoes population as a result of using the MHS inside the three blocks of flats. Therefore it can be expressed using the following equation:

$$P^* = \frac{12x}{12x + o + y}, \quad (5.1)$$

where x , o and y are defined as before. In this case $o = 356$ and $y = 1,524$. By using Eq. (5.1) and substituting all the values for x , o and y , we will be able to find the corresponding P^* in each case. The P^* values for each case are 0, 0.6871 and 0.7789, respectively.

In the next section, we will show some simulations produced in R for each case. Note that we will focus on two different P values mentioned in Table 4, namely $P = 0.1280$ and $P = 0.6610$ as these two are the two extreme P values. Unless stated otherwise, the unit of time is in weeks.

5.1. $P = 0.1280$

Let us recall again that

- (1) $P^* = 0$, no MHSs,
- (2) $P^* = 0.6871$, there are 344 MHSs and 356 ovitraps within the flats,
- (3) $P^* = 0.7789$, there are 552 MHSs and 356 ovitraps within the flats.

The results for number of incidence cases and the total number of dengue cases within the flats are shown in Fig. 4. The number of susceptible and infected mosquitoes within the flats are shown in Fig. 5. From Fig. 5, we can see that by introducing MHSs in the blocks of flats, the number of susceptible and infected mosquitoes have reduced drastically. From Fig. 4, we can see clearly the effectiveness of having MHSs within the blocks of flats by seeing a huge reduction in the number of incidence cases as well as the total number of dengue cases. The P^* value that performs the best by having the lowest number of infected individuals and number of incidence cases is when we have 552 MHSs inside the flats, namely when $P^* = 0.7789$ as expected.

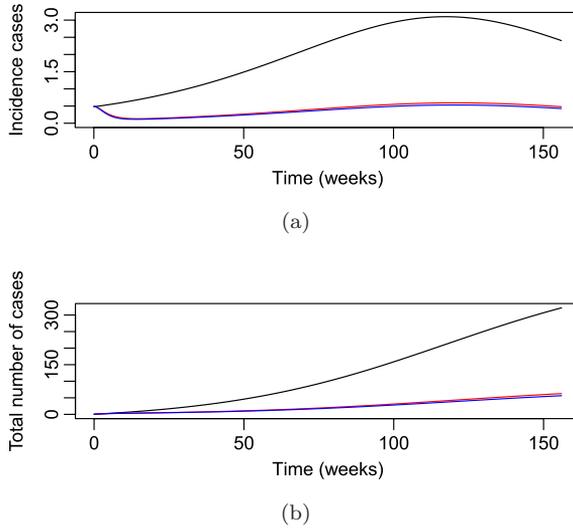


Fig. 4. Numerical simulations for (a) incidence cases (in weeks) and (b) total number of dengue cases within the flats for $P = 0.1280$ where the black line, red line and blue line represent $P^* = 0$, $P^* = 0.6871$ and $P^* = 0.7789$ respectively over a period of three years.

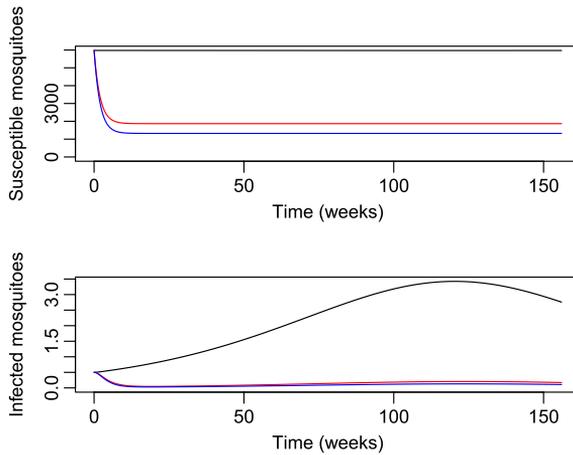


Fig. 5. Numerical simulation for the dynamical behavior of *Aedes* mosquitoes within the flats for $P = 0.1280$ where the black line, red line and blue line represent $P^* = 0$, $P^* = 0.6871$ and $P^* = 0.7789$ respectively over a period of three years.

5.2. $P = 0.6610$

Similarly, we will carry out the same procedure for when $P = 0.6610$. The results for number of incidence cases and the total number of dengue cases within the flats are shown in Fig. 6. The number of susceptible and infected mosquitoes within the flats are shown in Fig. 7. Similarly, from Fig. 7, we can see that by introducing the

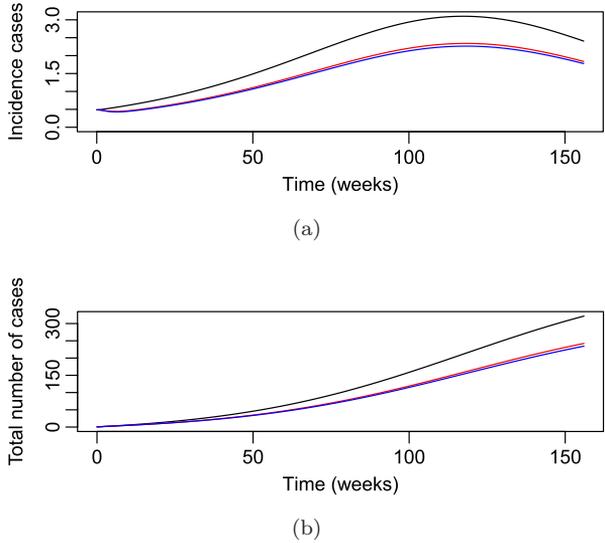


Fig. 6. Numerical simulations for (a) incidence cases (in weeks) and (b) total number of dengue cases within the flats for $P = 0.6610$ where the black line, red line and blue line represent $P^* = 0$, $P^* = 0.6871$ and $P^* = 0.7789$, respectively, over a period of three years.

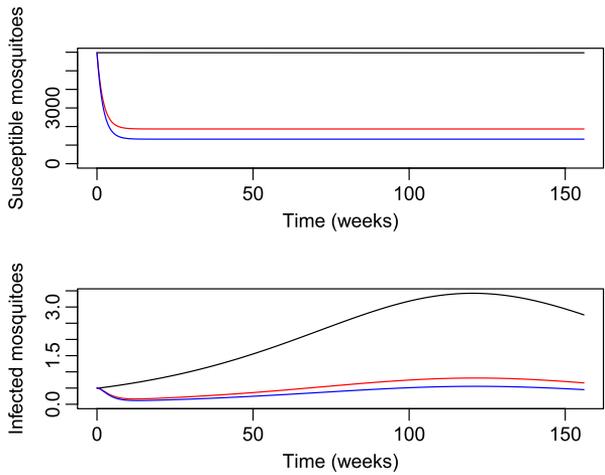


Fig. 7. Numerical simulation for the dynamical behavior of *Aedes* mosquitoes within the flats for $P = 0.6610$ where the black line, red line and blue line represent $P^* = 0$, $P^* = 0.6871$ and $P^* = 0.7789$ respectively, over a period of three years.

MHSs in the blocks of flats, the number of susceptible and infected have reduced. Again similarly, the number of incidence cases as well as the total number of dengue cases are reduced as a result of the MHSs as shown in Fig. 6. The P^* value that performs the best by having the lowest number of infected mosquitoes is when we have 552 MHSs inside the flats, namely when $P^* = 0.7789$.

5.3. Effect of P^* on spread of dengue in flats

In order for us to examine the effect that each P^* has on the spread of dengue within the flats, we will now look at the mean values for each variable. The results for various P values and P^* values are given in Tables 6, 8, 10 and 12 where their corresponding endemic equilibrium values are given in Tables 7, 9, 11 and 13, respectively.

From Table 6 where $P = 0.1280$, we can see that as P^* increases, the number of infected individuals, incidence cases, susceptible mosquitoes, infected mosquitoes and latent mosquitoes all decrease accordingly. If we compare this to the results given in Table 8 where $P = 0.3190$, then we can see that although those variables still decrease as P^* increases, the relative change is not as significant compared to when $P = 0.1280$.

Table 6. Mean values for variables within the flats for $P = 0.1280$, where $P^* = 0$: No MHSs, $P^* = 0.6871$: 344 MHSs and 356 ovitraps and $P^* = 0.7789$: 552 MHSs and 356 ovitraps to 3 d.p over one year.

$P = 0.1280$					
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	Total number of cases
0	2,946.550	0.912	252.538	0.933	48.984
0.6871	2,960.740	0.209	239.051	0.206	11.170
0.7789	2,961.215	0.190	238.595	0.186	10.151

P^* values	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0	5,973.959	0.745	0.966
0.6871	2,027.497	0.077	0.101
0.7789	1,500.067	0.059	0.078

Table 7. Endemic equilibrium values for variables within the flats for $P = 0.1280$, where $P^* = 0$: No MHSs, $P^* = 0.6871$: 344 MHSs and 356 ovitraps and $P^* = 0.7789$: 552 MHSs and 356 ovitraps to 3 d.p.

$P = 0.1280$					
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	Total number of cases per year
0	2,753.155	0.115	446.730	0.115	5.958
0.6871	3,106.745	0.024	93.231	0.024	1.243
0.7789	3,117.158	0.021	82.821	0.021	1.105

P^* values	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0	5,975.466	0.098	0.127
0.6871	1,869.773	0.006	0.008
0.7789	1,321.212	0.004	0.005

Table 8. Mean values for variables within the flats for $P = 0.3190$, where $P^* = 0$: No MHSs, $P^* = 0.6871$: 344 MHSs and 356 ovttraps and $P^* = 0.7789$: 552 MHSs and 356 ovttraps to 3 d.p over one year.

$P = 0.3190$					
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	Total number of cases
0	2,946.55	0.912	252.538	0.933	48.984
0.6871	2,956.848	0.404	242.748	0.407	21.667
0.7789	2,957.457	0.376	242.167	0.379	20.178

P^* values	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0	5,973.959	0.745	0.966
0.6871	2,027.385	0.126	0.164
0.7789	1,499.99	0.093	0.121

Table 9. Endemic equilibrium values for variables within the flats for $P = 0.3190$, where $P^* = 0$: No MHSs, $P^* = 0.6871$: 344 MHSs and 356 ovttraps and $P^* = 0.7789$: 552 MHSs and 356 ovttraps to 3 d.p.

$P = 0.3190$					
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	Total number of cases per year
0	2,753.155	0.115	446.730	0.115	5.958
0.6871	2,997.889	0.052	202.059	0.052	2.695
0.7789	3,013.21	0.048	186.742	0.048	2.491

P^* values	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0	5,975.446	0.098	0.127
0.6871	1,869.755	0.014	0.018
0.7789	1,321.20	0.009	0.012

Table 10. Mean values for parameters within the flats for $P = 0.4770$, where $P^* = 0$: No MHSs, $P^* = 0.6871$: 344 MHSs and 356 ovttraps and $P^* = 0.7789$: 552 MHSs and 356 ovttraps to 3 d.p over one year.

$P = 0.4770$					
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	Total number of cases
0	2,946.55	0.912	252.538	0.933	48.984
0.6871	2,954.022	0.545	245.434	0.553	29.228
0.7789	2,954.608	0.517	244.875	0.524	27.740

P^* values	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0	5,973.959	0.745	0.966
0.6871	2,027.304	0.162	0.210
0.7789	1,499.932	0.118	0.153

Table 11. Endemic equilibrium values for variables within the flats for $P = 0.4770$, where $P^* = 0$: No MHSs, $P^* = 0.6871$: 344 MHSs and 356 ovttraps and $P^* = 0.7789$: 552 MHSs and 356 ovttraps to 3 d.p.

$P = 0.4770$					
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	Total number of cases per year
0	2,753.155	0.115	446.730	0.115	5.958
0.6871	2,925.803	0.070	274.127	0.070	3.656
0.7789	2,940.294	0.067	259.640	0.067	3.463

P^* values	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0	5,975.446	0.098	0.127
0.6871	1,869.744	0.019	0.024
0.7789	1,321.192	0.013	0.016

Table 12. Mean values for variables within the flats for $P = 0.6610$, where $P^* = 0$: No MHSs, $P^* = 0.6871$: 344 MHSs and 356 ovttraps and $P^* = 0.7789$: 552 MHSs and 356 ovttraps to 3 d.p over one year.

$P = 0.6610$					
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	Total number of cases
0	2,946.55	0.912	252.538	0.933	48.984
0.6871	2,951.10	0.689	248.211	0.702	36.991
0.7789	2,951.552	0.667	247.781	0.680	35.822

P^* values	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0	5,973.959	0.745	0.966
0.6871	2,027.22	0.198	0.257
0.7789	1,499.871	0.145	0.188

Table 13. Endemic equilibrium values for variables within the flats for $P = 0.6610$, where $P^* = 0$: No MHSs, $P^* = 0.6871$: 344 MHSs and 356 ovttraps and $P^* = 0.7789$: 552 MHSs and 356 ovttraps to 3 d.p.

$P = 0.6610$					
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	Total number of cases per year
0	2,753.155	0.115	446.730	0.115	5.958
0.6871	2,855.752	0.088	344.160	0.088	4.590
0.7789	2,866.451	0.086	333.463	0.086	4.447

P^* values	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0	5,975.446	0.098	0.127
0.6871	1,869.733	0.024	0.031
0.7789	1,321.184	0.016	0.021

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From Tables 6, 8, 10 and 12, for a higher value of P , in other words, individuals are getting bitten more when going outside at certain time intervals, they are more likely to bring in new infections into the flats. Although using the MHSs within the blocks of flats reduced the number of infected individuals as well as the number of incidence cases, the effect decreases as P increases. This is to be expected as smaller P values represent the individuals spending relatively more time in the flats so the effect of the MHSs is bigger (for the same value of P^*).

Nonetheless, it is important to note that the MHSs are effective in reducing and controlling the spread of dengue within the blocks of flats both in the short run and in the long run.

5.4. Starting at endemic equilibrium

In this section, we will continue to examine the effect of having different number of MHSs within the flats when our population starts at the endemic equilibrium (EE) in the absence of MHSs. Let us define the EE initial values as follows:

$$\begin{aligned}
 S_{H_1}(0) &= 1,479,821, & I_{H_1}(0) &= 61.569, & R_{H_1}(0) &= 240,117.60, \\
 S_{v_1}(0) &= 3,211,802, & L_{v_1}(0) &= 52.546, & I_{v_1}(0) &= 68.171, \\
 S_{H_2}(0) &= 2,753.155, & I_{H_2}(0) &= 0.115, & R_{H_2}(0) &= 446.730, \\
 S_{v_2}(0) &= 5,975.446, & L_{v_2}(0) &= 0.098, & I_{v_2}(0) &= 0.127,
 \end{aligned}$$

where all the parameter values are defined as before. Note that the above EE initial values are obtained from numerical simulations where $P^* = 0$.

The effects of introducing the MHSs into the flats when the population system is at endemic equilibrium are illustrated in both Tables 14 and 15 for when $P = 0.1280$ and $P = 0.6610$, respectively. For both cases, we noticed a drastic decrease in the number of infected individuals within the blocks of flats when we first introduced the MHSs (82.36% decrease for $P = 0.1280$ and 26.02% decrease for $P = 0.6610$). When we increase the number of MHSs from 344 to 552, although the number of infected individuals have been reduced further, the relative changes are not as significant (a further decrease of 9.93% for $P = 0.1280$ and 3.36% for $P = 0.6610$).

Table 14. Variable values within the flats for $P = 0.1280$, where $P^* = 0.6871$: 344 MHSs and 356 ovitraps and $P^* = 0.7789$: 552 MHSs and 356 ovitraps to 3 d.p over a period of 52 weeks with initial values starting at EE.

$P = 0.1280$							
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0.6871	2,757.571	0.020	442.409	0.020	1,869.775	0.005	0.007
0.7789	2,757.706	0.018	442.276	0.018	1,321.213	0.003	0.004

Table 15. Variable values within the flats for $P = 0.6610$, where $P^* = 0.6871$: 344 MHSs and 356 oitraps and $P^* = 0.7789$: 552 MHSs and 356 oitraps to 3 d.p over a period of 52 weeks with initial values starting at EE.

$P = 0.6610$							
P^* values	$S_{H_2}(t)$	$I_{H_2}(t)$	$R_{H_2}(t)$	Incidence cases	$S_{v_2}(t)$	$L_{v_2}(t)$	$I_{v_2}(t)$
0.6871	2,754.569	0.085	445.346	0.085	1,869.735	0.023	0.029
0.7789	2,754.708	0.082	445.210	0.082	1,321.185	0.015	0.020

Nonetheless, it is reassuring to see that the MHSs are effective even when the population system is already at endemic equilibrium level.

5.5. Endemic equilibrium

Another way in which we can examine the effect of using the MHSs within the flats and later deploy them throughout Malaysia would be to look at the endemic equilibrium (EE) level. In this section, we will compare the endemic equilibrium level when we have no MHSs within the flats and when we have the MHSs within the three blocks of flats. In this section, we will set $P = 0.6610$ where this P value represents people spending time outdoors between 6 am and 7.45 pm.

For the case when we have no MHSs in the flats, in other words when $P^* = 0$, the endemic equilibrium value for the number of infected individuals in KL and in the flats are 61.569 and 0.115, respectively to 3 d.p.

For the case when we have introduced 552 MHSs inside the three blocks of flats, we have that the endemic equilibrium points for the number of infected individuals in KL and in the flats are 61.569 and 0.086, respectively to 3 d.p.

From the above results, we can see that although by having the MHSs inside the flats has reduced the endemic equilibrium level for the number of infected individuals within the flats by around 25%, we notice an insignificant change in the endemic equilibrium level for the number of infected individuals in KL. This indicates that although the MHSs have successfully reduced the number of dengue cases within the flats, in order to achieve extinction within the whole of KL and thus later to the whole of Malaysia, more MHSs would need to be deployed in more places throughout KL.

Table 16 illustrates the effect of having different P and P^* values on the number of incidence cases at EE.

From Table 17, we can see clearly that as P increases, the percentage reduction in the average number of incidence cases from when we have 344 MHSs within the flats to 552 MHSs decreases. In other words, if individuals who reside within the blocks of flats go outdoors the majority of the time and thus get bites from outdoors, the effect from increasing the number of the MHSs within the flats gets reduced. Putting this in a non-mathematical context, if the majority of the people resident in the blocks of flats are in KL between 6 am to 7.45 pm, then the difference between

Table 16. Number of of incidence cases per week at EE for different number of MHSs within the flats for different proportions of time spent outdoors.

<i>P</i> values	0 MHSs	344 MHSs	554 MHSs
0.1280	0.115	0.024	0.021
0.3190	0.115	0.052	0.048
0.4770	0.115	0.070	0.067
0.6610	0.115	0.088	0.086

Table 17. Percentage reduction in the average number of incidence cases for various values of *P* within the flats at EE.

<i>P</i> values	<i>P</i> * = 0–0.6871	<i>P</i> * = 0.6871–0.7789
0.1280	79.13%	12.50%
0.3190	54.78%	7.69%
0.4770	39.13%	4.29%
0.6610	23.48%	2.27%

using 344 MHSs and 552 MHSs is only 2.27% difference in the average number of incidence cases with an impact ratio of only 0.0227.

6. Discussion and Conclusion

In this paper, we have used the classic Ross–Macdonald model⁶ to describe the spread of dengue in Malaysia between human and *Aedes* mosquitoes. Note that the classic Ross–Macdonald model⁶ was based on analyzing the *Anopheles* mosquito, which is responsible for transmitting malaria. However, over the past years, many researchers have also used the classic Ross–Macdonald model⁶ to describe the spread of other vector-borne diseases, most specifically on dengue, for example.^{8,23–25}

By using the MHSs trial data collected in the three blocks of flats in Selangor,⁷ we have performed different analyses to investigate the effect of using different numbers of MHSs on the number of dengue cases in the trial site. In Sec. 3, we have mathematically estimated the number of potential *Aedes* breeding sites which will help us in deciding the correct number of MHSs that we would need to deploy to control the spread of dengue. From the numerical simulations produced throughout this paper, it is clear that using the MHS does indeed reduce the number of susceptible and infected mosquitoes. As a result, the MHSs have effectively reduced the number of incidence cases within the trial sites and thus reduced the number of dengue cases within that area. Our results have suggested that by using the MHSs in a high-rise condominium environment, the number of dengue cases have reduced, which is very promising.

It is important to note, however, that despite the effectiveness in reducing the number of dengue cases within the blocks of flats, it shows very little effect in reducing the number of dengue cases in KL as a whole. This is to be expected as

the effect from the three blocks of flats is not significant enough to cause an overall impact to KL especially when dengue is endemic in Malaysia. This implies that, in order to achieve the effect that we experienced in the three blocks of flats, we would need to deploy MHSs in other areas in KL.

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